Interregional Redistribution and Budget Institutions under Asymmetric Information

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Abstract: Empirical evidence from the U.S. and the European Union suggests that regions which contribute to interregional redistribution face weaker borrowing constraints than regions which benefit from interregional redistribution. This paper presents an argument in favor of such differentiated budgetary institutions. It develops a two-period model of a federation consisting of two types of regions. The federal government redistributes from one type of regions (contributors) to the other type (recipients). It is shown that a fiscal constitution with lax budget rules for contributors and strict budget rules for recipients solves the self-selection problem the federal government faces in the presence of asymmetric information regarding exogenous characteristics of the regions.

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key words: asymmetric information, interregional redistribution, borrowing rules

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1 Introduction

Constraints on public borrowing are widespread among U.S. states. The National Association of State Budget Office (1992) reports that all states but Vermont have statutory or constitutional balanced budget requirements or debt limits. But there is a large variation in the stringency of such budget institutions. For instance, some states exempt special programs like capital funds, some states are allowed to issue short-term debt carrying over deficits to the next fiscal year, and some states may borrow on the behalf of a public referendum. Poterba (1996) argues that anti-deficit rules are usually more stringent in small states than in large states. Furthermore, it is well known that federal taxes and transfers in the U.S. redistribute resources from high-income to low-income states (e.g. Bayoumi and Masson, 1995, Mélitz and Zumer, 2002). Taken together these two observations we may conclude that, ceteris paribus, states which contribute to interregional redistribution face weaker borrowing constraints than states which benefit from interregional redistribution.

There is a similar budget institution in the European Union. The Stability and Growth Pact (SGP) restricts the annual deficit of member states to 3% of GDP. If a country violates this requirement, the Council of the European Union may initiate an institutional procedure which induces the country to bring down its deficit. In recent years, an increasing number of member states did not satisfy the deficit criterion and a hot debate about the SGP started. In light of this experience, the Council recently legislated a regulation on clarifying the excessive deficit procedure. One important change is that in identifying an excessive deficit "... special consideration shall be given to budgetary efforts towards increasing or maintaining at a high level financial contributions to fostering international solidarity and to achieving European policy goals, notably the unification of Europe ..." (Council of the European Union, 2005). This amendment inter alia aims at the member countries’ (net) payments to the budget of the union. Since one of the main purposes of this budget is to redistribute between member states, we come to a similar conclusion as for the U.S.: Contributors in the European Union are subject to weaker borrowing constraints than recipients.

While such a weakening of deficit limits is problematic from a monetary point a view, as it usually leads to higher inflation and interest rates (e.g. Feldstein, 2005), the present paper argues that a fiscal constitution with strict borrowing rules for recipient countries
and lax borrowing rules for contributing countries of a federation may nonetheless beneficial, if considered in the realm of fiscal federalism. Our main argument in favor of differentiated budget rules is that it can solve the self-selection problem a federal government faces in the presence of asymmetric information. We develop a two-period model of a federation in which the federal government (center) redistributes from one type of regions (contributors) to the other type (recipients). Each region finances its supply of a local public good by an income tax and public debt. The types of regions differ in an exogenously given characteristic. In our basic model, we focus on different rates of time preference. In a modified model, it is argued that the results remain completely unchanged under other sources of heterogeneity, for example, differences in the cost of regional public services or differences in labor productivity.

In this fiscal federalism model, we first characterize the welfare optimum under full and asymmetric information. In the latter case, the exogenously given characteristic is private information of the regions and cannot be observed by the federal government. It is then shown that the federal government can implement the full information optimum by a simple redistribution scheme consisting of lump-sum taxes and transfers. But under asymmetric information, incentive compatibility requires that the federal government distorts the intertemporal allocation in recipient states in favor of future public consumption. It therefore cannot implement the asymmetric information optimum by the simple redistribution system. Efficiency is attained, however, if the redistribution scheme is augmented by a limit on public borrowing in recipient regions. The limit restricts current spending and effectively shifts public consumption from the present to the future. Since it applies to recipients only, budget institutions in the federation are more stringent for recipients than for contributors.

This result has normative as well as positive implications. The normative implications are important especially from an European point of view. The result shows that differentiated borrowing constraints for contributors and recipients in the European Union can be justified on efficiency grounds. This economic benefit of an institutional change in the excessive deficit procedure of the SGP has to be balanced against possible drawbacks. The positive implications are relevant especially for the U.S. states. While a lot of studies identify the impact of different budget institutions on e.g. the states’ spending behavior (e.g. von Hagen, 1991, Poterba, 1994, 1995, 1996, and Poterba and
Rueben, 2001), to the best of our knowledge no attention has been paid to the question why states face different borrowing restrictions. We will interpret our result as a pork barrel policy. A state is supported by redistribution, but only if it is willing to accept and implement a stringent budget rule. This argument may help to explain the variation in the stringency of budget institutions among U.S. states.

The driving force of our results is the assumption of asymmetric information. This assumption is based on empirical grounds. For example, in determining a Ramsey-type social discount rate for six major countries, Evans and Sezer (2004) have to figure out the elasticity of marginal utility of consumption \((e)\), the long-run growth rate of per-capita consumption \((g)\) and the pure rate of time preference \((p)\). While presenting rigorous econometric estimates of \(e\) and \(g\), they recognize "... the difficulty of settling on a suitable measure of \(p\) . . ." (p. 558) and make assumptions on the appropriate value of \(p\). If it is difficult for researchers to assess the rate of time preference of major countries, it will also hardly be possible for federal governments to infer this rate in the regions of a federation. Similar evidence on asymmetric information regarding other regional characteristics can be found in previous literature which we will now turn to.

Our analysis is related to two lines of economic literature. First, there is an extensive and interesting literature on asymmetric information in federations. This literature discusses optimal interregional redistribution under asymmetric information with respect to income or the preference for public goods (Lockwood, 1999), the cost of public goods (Lockwood, 1999, Cornes and Silva, 2002) and labor productivity (Raff and Wilson, 1997, Bordignon et al. 2001). Cremer et al. (1996) consider the case where both income and the preference for a public good are private information of the regions. The consequence of asymmetric information in a tax competition framework is analyzed in Bucovetsky et al. (1998). Cornes and Silva (2003) determine the optimal spending mix under private information and Huber and Runkel (2005) use the self-selection approach to rationalize specific types of intergovernmental grants. But all these articles use one-period models and, thus, do not capture the implications of asymmetric information for regional public debt and the design of budget institutions in a federation.

Second, our paper is also related to the literature on budget institutions. For example, the literature on the political economy of public debt provides arguments in favor of borrowing rules. Tabellini and Alesina (1990) and Alesina and Tabellini (1990) show
that political instability leads to time-inconsistent preferences of policy makers and so gives rise to excessive and ex-ante inefficient deficits. A balanced budget rule serves as commitment device and restores efficiency. Peletier et al. (1999) extend this framework and argue that a balanced budget rule causes inefficient underinvestment of the public sector. They propose a ‘Golden Rule of Public Finance’ requiring the public deficit to be not larger than public investment. An overview of these and related studies on fiscal institutions is given by Alesina and Perotti (1999). But all previous articles do not discuss public debt and interregional redistribution under asymmetric information and, thus, do not provide a self-selection rationale for differentiated budget rules.\(^1\)

The paper is organized as follows. As a further motivation, in Section 2 we discuss the evidence from the European Union and the U.S. in more detail. Section 3 describes the basic theoretical model. In Section 4 and 5, we derive the welfare optimum and show how this optimum can be implemented by a suitable federal redistribution scheme. Section 6 briefly discusses the robustness of the results, and Section 7 concludes.

\section{Empirical Evidence}

The evidence from the European Union is clear. According to the legislated regulation referred to in the introduction, in the future the excessive debt procedure ceteris paribus will be less restrictive for contributors than for recipients. The 3\%-criterion will be strictly applied to the recipient countries, while contributing countries face a borrowing limit which effectively is larger than 3\% of GDP. Moreover, we can argue that there have already been differentiated budget institutions in the past. The excessive deficit procedure is not an automatic mechanism, but to a large part it is at the discretion of the Council to judge whether a deficit above 3\% of GDP represents an excessive deficit. A lot of exemptions allow a country to run a higher deficit. Hence, the political power of a member state in the Council may be viewed as a proxy for the stringency of the deficit limit which the SGP imposes on this state. Barr and Passarelli (2004) compute a Shapley-Shubik Index (SSI) which gives the political power of the EU-15

\(^1\)Regional debt is analyzed in the models of Goodspeed (2002) and Schultz and Sjöström (2001, 2004). But the former author focusses on bailouts in federations and the latter discuss the relation of migration and debt. They do not refer to the budget institutions considered in our paper.
countries in the Council. Figure 1 plots this index against the net balance (NBAL) during the years 1999-2003, i.e. the difference between payments from and payments to the European budget as a percentage of GDP (Heinemann, 2005).

Although the sample is too small to run a reliable econometric estimation, the figure yet shows that recipient states tend to have lower political power and, thus, a stricter debt limit than contributing states, at least than the large contributors like Italy, UK, Germany and France. This view is supported by the experience we made with the enforcement of the excessive deficit procedure. As Portugal, one of the main beneficiaries of redistribution in the European Union, violated the 3%-criterion in 2002, it was forced by the Council to bring down its deficit. The breach of the deficit criterion by Germany and France in 2003 was also punished by initiating the deficit procedure, indeed, but as the countries did not follow the recommendation of the Council a long and hot debate about the SGP emerged and in the end the pact was weakened.

The evidence from the U.S. is less obvious since, strictly speaking, there is no such explicit redistribution system as in Europe. However, it is well known that federal taxes and transfers implicitly redistribute resources between the states. For example, Bayoumi and Masson (1995) and Méliot and Zumer (2002) define a state’s relative per capita personal income as that state’s per capita personal income divided by the average per capita personal income of all states. They estimate the relation between
the relative incomes before and after federal taxes and transfers. The results suggest that the U.S. federal government redistributes about 20 cent of every dollar difference in pre-tax incomes. Hence, redistribution from states with above average income to states with below average income is clearly an element of the U.S. tax system.

To bridge the gap to our analysis of interregional redistribution and budget institutions, we will now estimate the impact of the relative per capita income on the stringency of borrowing rules in the U.S. states. Data on per capita personal income from 1969 to 2004 are provided by the U.S. Commerce Department. With the help of these data, we compute the variable RELINC which gives a state’s relative per capita personal income before federal taxes and transfers. For each state, we take the average of this variable over the whole time period 1969 to 2004. Data on the stringency of budgetary institutions are available from the Advisory Council of Intergovernmental Relations (1987, 1998) and Poterba and Rueben (2001). They provide an index BUD-STR ranging from 0 (lax budget rules) to 10 (stringent budget rules). The scatterplot in Figure 2 illustrates the relation between BUDSTR and RELINC.

The plot suggests that high-income states (contributors) really tend to have weaker borrowing rules than low-income states (recipients). This hypothesis can be tested by a simple probit regression. RELINC is taken as the independent variable. As dependent variable we construct an indicator BUDIND that receives the value 1, if BUDSTR is
9 or 10. BUDIND is set equal to zero, if BUDSTR is below 9. Since the mean of BUDSTR lies between 8 and 9, BUDIND divides the set of all states into states with above average budget stringency and states with below average budget stringency. A further motivation for BUDIND is that a state scores a 9 or 10 for BUDSTR only if it requires a strict balanced budget at the end of the fiscal year. A value of 8 for BUDSTR already indicates that the state is allowed to run a short-run deficit. If BUDIND is equal to zero (one), the borrowing constraint is said to be weak (strict).

The results of our probit regression are displayed in Table 1. The coefficient of

<table>
<thead>
<tr>
<th>Dependent variable: BUDIND</th>
<th>coeff.</th>
<th>std.err.</th>
<th>z-statistic</th>
<th>p-value</th>
<th>95% conf. interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>constant</td>
<td>6.035</td>
<td>1.674</td>
<td>3.60</td>
<td>0.000</td>
<td>[2.753; 9.316]</td>
</tr>
<tr>
<td>RELINC</td>
<td>-5.786</td>
<td>1.645</td>
<td>-3.52</td>
<td>0.000</td>
<td>[-9.010; -2.563]</td>
</tr>
</tbody>
</table>

Notes: (i) observations: 50, (ii) log likelihood = -26.306, (iii) pseudo R² = 0.227.

RELINC is of the expected sign and statistically significant at the one percent level. To assess the economic significance, we define the average recipient (contributor) as the state with average per capita income among all states with RELINC < 1 (RELINC > 1). It is then straightforward to compute the predicted probability of the average recipient having a strict budget rule as 81.20%. In contrast, the average contributor faces a strict borrowing constraint with a probability of 32.97% only. Hence, also in the U.S. there is clear evidence that borrowing restrictions tend to be weaker in states which contribute to interregional redistribution than in other states.

3 Theoretical Model

We consider a two-period model of a federation consisting of a federal government and several regions. There are two types of regions indexed by $s$ and $h$. The number of type

\cite{Poterba and Rueben (2001)} use a similar indicator variable, but draw the line of demarcation between weak and strict budget institutions at BUDSTR = 6. Under this indicator variable our empirical results slightly change, but the main conclusion remains the same.
s and type h regions is denoted by \( m_s \geq 1 \) and \( m_h \geq 1 \), respectively. The difference between the types of regions will be explained below. For the time being, we note that each region is populated by a cohort of \( n \) identical individuals which live for one period only. After the period 1 cohort has passed away, in period 2 there is a new cohort of exactly the same size. In period \( t = 1, 2 \), an individual in a region of type \( i = s, h \) consumes \( c_{ti} \) units of a private good, \( g_{ti} \) units of a local public good supplied by the regional government and \( x_{ti} = 1 - \ell_{ti} \) units of leisure. \( \ell_{ti} \) is the individual’s labor supply. Utility of the individual is given by

\[
 u_i = c_{ti} + W(x_{ti}) + U(g_{ti}). \tag{1}
\]

The functions \( W \) and \( U \) satisfy \( W_x > 0 \), \( W_{xx} < 0 \), \( U_g > 0 \) and \( U_{gg} < 0 \), where subscripts indicate partial derivatives. Utility is assumed to be quasi-linear in order to abstract from income effects in the supply of the local public good. In period \( t \), the representative individual in region \( i \) maximizes utility (1) subject to the budget constraint \( c_{ti} = (1 - \tau_{ti})\ell_{ti} \), where \( \tau_{ti} \) is the tax rate of an income tax imposed by the local government. The first-order condition of utility maximization is

\[
 1 - \tau_{ti} - W_x(1 - \ell_{ti}) = 0. \tag{2}
\]

It determines the individual’s optimal labor supply as a function of the local tax rate, i.e. \( \ell_{ti} = L(\tau_{ti}) \) with \( L'(\tau_{ti}) = 1/W_{xx} < 0 \) and \( L''(\tau_{ti}) = W_{xxx}/(W_{xx})^3 < 0 \).

Inserting the optimal labor supply in (1) gives the indirect utility function of the representative individual in region \( i \) and period \( t \). The present value of region \( i \)'s (per capita) welfare can then be written as

\[
 v_i = (1 - \tau_{1i})L(\tau_{1i}) + W[1 - L(\tau_{1i})] + U(g_{1i})
 + \delta_1 \left[ (1 - \tau_{2i})L(\tau_{2i}) + W[1 - L(\tau_{2i})] + U(g_{2i}) \right]. \tag{3}
\]

\(^3\)Note that \( W_x > 0 \) and \( W_{xx} < 0 \) imply \( W_{xxx} > 0 \), provided all derivatives of \( W \) are monotone for \( x \geq 0 \) (Menegatti, 2001). The most frequently used utility functions have monotone derivatives, for instance, the CES function \( W(x) = (x^{1-\alpha} - 1)/(1 - \alpha) \) with \( \alpha \in]0, 1[ \), which for \( \alpha = 1 \) encompasses the logarithmic function \( W(x) = \ln(1 + x) \), and the exponential function \( W(x) = 1 - \exp{-\alpha x} \) with \( \alpha > 0 \). A counterexample is \( W(x) = \alpha x - \beta x^2 \) with \( x < \alpha/2\beta \) and \( \alpha, \beta > 0 \). This function implies \( W_{xxx} = 0 \). But we then obtain \( L_{\tau\tau} = 0 \) and all our subsequent results remain true.
\( \delta_i = 1/(1 + \rho_i) \in [0,1] \) denotes the discount factor and \( \rho_i \geq 0 \) is the discount rate or, equivalently, the rate of time preference in region \( i \). We assume \( \delta_s < \delta_h \). A region of type \( s \) has a smaller discount factor (a higher discount rate) than a region of type \( h \). Type \( s \) regions discount the future more and place lower weight on the well-being of future generations than type \( h \) regions. Thus, \( \delta_i \) can also be interpreted as an intergenerational altruism parameter of the first-period inhabitants of region \( i \).

In each period, the local government of a type \( i \) region finances its public good supply by the revenue of the income tax. Moreover, in period 1 it additionally receives a transfer \( z_i \) from the central government and may issue debt \( b_i \). The debt plus interest payments has to be paid back in period 2. We assume that all regions borrow on the world capital market and take as given the interest rate \( r \geq 0 \). The local government’s budget constraints in period 1 and 2 can be written as, respectively,

\[
ge_{1i} = n \tau_1 L(\tau_1) + b_i + z_i, \quad g_{2i} = n \tau_2 L(\tau_2) - (1 + r)b_i. \tag{4}
\]

The transfer from the center is not restricted in sign. If it is negative, it represents a tax that the federal government imposes on a type \( i \) region. As we explain in more detail below, the sole objective of the center is to optimally redistribute between the regions. Its budget constraint reads

\[
m_s z_s + m_h z_h = 0. \tag{5}
\]

This budget constraint completes the model. It implies that the center collects resources from one type of regions to finance the transfers to the other type of regions.\(^4\)

For the proofs of our results, it is useful to determine the properties of a region’s preferences in the debt-transfer space. For this, we maximize region \( i \)’s welfare \((3)\) with respect to the first- and second-period income tax rates and, for the time being, take as given debt and the federal transfer. The result is the region’s welfare function

\[
V(b, z, \delta) = \max_{\tau_1, \tau_2} \left\{ (1 - \tau_1)L(\tau_1) + W[1 - L(\tau_1)] + U[n \tau_1 L(\tau_1) + b + z] \\
+ \delta [(1 - \tau_2)L(\tau_2) + W[1 - L(\tau_2)] + U[n \tau_2 L(\tau_2) - (1 + r)b]] \right\}, \tag{6}
\]

\(^4\)Attention is restricted to redistribution in period 1 since we are interested in the relation between redistribution and public borrowing, the latter taking place also in the first period only. But it is straightforward to show that our main results are not affected, if the federal government is supposed to redistribute in the second period or in both periods.
where, for notational convenience, the region index \( i \) is suppressed. The first-order conditions of the maximization problem in (6) can be written as

\[
\begin{align*}
    nU_g(g_1) &= 1 - \frac{\tau_1 L_r(\tau_1)}{L(\tau_1) + \tau_1 L_r(\tau_1)}, \quad nU_g(g_2) = 1 - \frac{\tau_2 L_r(\tau_2)}{L(\tau_2) + \tau_2 L_r(\tau_2)},
\end{align*}
\]

(7) with \( g_1 = n\tau_1 L(\tau_1) + b + z \) and \( g_2 = n\tau_2 L(\tau_2) - (1 + r)b \). Equation (7) represents the well-known modified Samuelson rule for the provision of public goods in the presence of distortionary income taxation (e.g. Atkinson and Stiglitz, 1980). In each period, the sum of the marginal willingness to pay for the public good is equated to the marginal cost of the public good and the tax distortion cost. Hence, in our model the intratemporal supply of the public good is distorted by the income tax only, independent of the information structure. Equation (7) also implies \( L(\tau_t) + \tau_t L_r(\tau_t) > 0 \), i.e. the regions are always on the increasing side of the Laffer curve.

Equation (7) determines the region’s optimal income tax rates as functions of debt and the federal transfer. Formally, we have \( \tau_1 = T^1(b, z) \) and \( \tau_2 = T^2(b) \) with

\[
\begin{align*}
    T^1_b(b, z) &= T^1_z(b, z) = -\frac{nU_g^1(L^1 + \tau_1 L^1_r)}{n^2(L^1 + \tau_1 L^1_r)^2U_g^1 + nU_g^1(2L^1_r + \tau_1 L^1_r^2)} - L^1_r > 0, \\
    T^2_b(b) &= \frac{n(1 + r)U_g^2(L^2 + \tau_2 L^2_r)}{n^2(L^2 + \tau_2 L^2_r)^2U_g^2 + nU_g^2(2L^2_r + \tau_2 L^2_r^2)} - L^2_r > 0,
\end{align*}
\]

(8) (9) where \( L^t := L(\tau_t), L^t_r := L_r(\tau_t), U^t_g := U_g(g_t) \) and so on. The denominators of (8) and (9) are negative due to the second-order conditions of the maximization problem (6). Equation (8) states that an increase in public borrowing or in the federal transfer allows to reduce the income tax rate in period 1. According to (9), higher debt requires a larger tax rate in period 2 since debt has to be repaid in the second period.

Applying the envelope theorem to the region’s welfare function (6), we obtain the slope of an indiﬁence curve in the \((b, z)\)-space

\[
\begin{align*}
    \frac{dz}{db}\bigg|_{av=0} &= \frac{U_g[n\tau_1 L(\tau_1) + b + z] - \delta(1 + r)U_g[n\tau_2 L(\tau_2) - (1 + r)b]}{U_g[n\tau_1 L(\tau_1) + b + z]},
\end{align*}
\]

(10) with \( \tau_1 = T^1(b, z) \) and \( \tau_2 = T^2(b) \). The curvature can be written as

\[
\begin{align*}
    \frac{d^2z}{db^2}\bigg|_{av=0} &= \frac{\delta^2(1 + r)^2[L^1 L^1_r + \tau_1 L^1 L^1_r^2 + \tau_1 (L^1_r)^2]U_g^2 L^1_b}{n(L^1 + \tau_1 L^1_r)^2(U_g^1)^3} \\
    &\quad - \frac{\delta(1 + r)[L^2 L^2_r + \tau_2 L^2 L^2_r^2 + \tau_2 (L^2_r)^2]T^2_b}{n(L^2 + \tau_2 L^2_r)^2U_g^1} > 0.
\end{align*}
\]

(11)
Hence, the indifference curve is U-shaped with the minimum at the point where the intertemporal rate of substitution equals the intertemporal rate of transformation, i.e. \( \frac{U_g(q_1)}{\delta U_g(q_2)} = 1 + r \). To understand the difference between a \( s \)-region indifference curve and a \( h \)-region indifference curve, differentiate (10) with respect to the discount factor. The result is

\[
\frac{d}{d\delta} \left( \frac{dV}{db} \bigg|_{dV=0} \right) = \frac{(1 + r)U_g^2}{U_g^1} > 0.
\]

\( \delta_h > \delta_s \) implies that, in every point in the \((b, z)\)-space, the indifference curve of a \( h \)-region has larger slope than the indifference curve of a \( s \)-region. This property represents the single-crossing property in our model. Two given indifference curves of \( h \)-regions and \( s \)-regions cross only once.

4 Welfare Optimum

In this section, we analyze the welfare maximizing policy of the federal government. In doing so, we consider two different information structures. As a benchmark, attention is paid to the case in which the federal government is able to observe all variables and characteristics of the regions. The associated welfare optimum is called full information optimum. In the second case, the rate of time preference is private information of the regions. The federal government cannot infer whether a region places low or high weight on the welfare of future generations. This asymmetric information assumption can be motivated by the empirical evidence referred to in the introduction. The resulting welfare optimum is the asymmetric information optimum.

The objective of the center is to maximize total welfare subject to its budget constraint. Under asymmetric information, it additionally takes into account incentive compatibility constraints which ensure that each region has a (weak) incentive to truthfully reveal its type.\(^5\) According to the revelation principle, the federal government offers each type of regions a contract stipulating the federal transfer and the region’s debt. Formally, the welfare maximization problem reads

\[
\max_{b_s, z_s, b_h, z_h} \ m_s V(b_s, z_s, \delta_s) + m_h V(b_h, z_h, \delta_h)
\]  

\(^5\)As usual in the fiscal federalism literature, participation constraints are ignored. The underlying assumption is that leaving the federation is prohibitively costly for a region.
subject to (5) and
\[ V(b_s, z_s, \delta_s) \geq V(b_h, z_h, \delta_s), \quad (IC_s) \]
\[ V(b_h, z_h, \delta_h) \geq V(b_s, z_s, \delta_h). \quad (IC_h) \]

(IC_s) and (IC_h) are the incentive constraints for s- and h-regions, respectively. (IC_s) requires that a s-region must not obtain lower utility from its own contract than from the contract offered to h-regions. An analogous interpretation applies to (IC_h).

In using the Utilitarian welfare function (13) we follow previous articles on self-selection in federation, for example, Cremer et al. (1996) and Bucovetsky et al. (1998). As in their model with heterogeneous public good preferences, this may raise conceptual issues. The Utilitarian function sums the welfare of all regions and places equal weight to both types of regions. Maximizing the function therefore yields one special point on the Pareto utility frontier of the federation. The use of the Utilitarian welfare function is nonetheless justified. It reveals the basic mechanism behind the general model. Moreover, in Section 6 we will argue that our main results remain unchanged, if the federal government places different weights to s- and h-regions and if the weight assigned to s-regions is not higher than a certain threshold value.

Using the envelope theorem, the first-order conditions to (13) can be written as
\[ (m_s + \mu_s) \left[ U_g(g_{1s}) - \delta_s(1 + r)U_g(g_{2s}) \right] - \mu_h \left[ U_g(g_{1s}) - \delta_h(1 + r)U_g(g_{2s}) \right] = 0, \quad (14) \]
\[ (m_h + \mu_h) \left[ U_g(g_{1h}) - \delta_h(1 + r)U_g(g_{2h}) \right] - \mu_s \left[ U_g(g_{1h}) - \delta_s(1 + r)U_g(g_{2h}) \right] = 0, \quad (15) \]
\[ (m_s + \mu_s - \mu_h)U_g(g_{1s}) - \lambda m_s = 0, \quad (16) \]
\[ (m_h + \mu_h - \mu_s)U_g(g_{1h}) - \lambda m_h = 0. \quad (17) \]

\( \lambda, \mu_s \) and \( \mu_h \) are the Lagrange multipliers associated with (5), (IC_s) and (IC_h), respectively. In addition to (14) to (17), we have to take into account the slackness conditions associated with the incentive constraints (IC_s) and (IC_h). Throughout we suppose the federal budget constraint is binding so that \( \lambda > 0 \).

As a benchmark, consider first the welfare optimum in case of full information. The center can directly observe the type of a region and ignores the incentive constraints. In (14) to (17) we have to set \( \mu_s \equiv \mu_h \equiv 0 \). Denoting optimal values under full information by the superscript 'o', we obtain
Proposition 1. The full information optimum satisfies

\[ \frac{U_i(g_{1i}^o)}{\frac{\delta_i U_i(g_{2i}^o)}{}} = 1 + r, \quad i \in \{s, h\} \]

and \(g_{1s}^o = g_{1h}^o, \tau_{1s}^o = \tau_{1h}^o, g_{2s}^o < g_{2h}^o, \tau_{2s}^o > \tau_{2h}^o, b_s^o > b_h^o\) and \(z_s^o < z_h^o\). Moreover, it satisfies (IC\(_h\)), but violates (IC\(_s\)).

**Proof:** \(U_g(g_{1i}^o)/\delta_i U_g(g_{2i}^o) = 1 + r, i \in \{s, h\}\), follows from (14), (15) and \(\mu_s \equiv \mu_h \equiv 0\). Inserting \(\mu_s \equiv \mu_h \equiv 0\) in (16) and (17) yields \(U_g(g_{1s}^o) = U_g(g_{1h}^o)\) and \(g_{1s}^o = g_{1h}^o\). Since (7) holds in both types of regions, we obtain \(\tau_{1s}^o = \tau_{1h}^o\). Using (16) and (17) in (14) and (15) yields \(\delta_i U_g(g_{2s}^o) = \delta_i U_g(g_{2h}^o)\). It follows \(U_g(g_{2s}^o) > U_g(g_{2h}^o)\) and \(g_{2s}^o < g_{2h}^o, \tau_{2s}^o > \tau_{2h}^o\) is then implied by (7) because \(F(\tau) := 1 - \tau L_0(\tau)/[L(\tau) + \tau L_1(\tau)]\) is an increasing function according to \(F_0(\tau) = [\tau(L_0)^2 - LL_0 - \tau LL_1]/(L + \tau L_1)^2 > 0\). \(g_{2s}^o < g_{2h}^o\) yields \((1 + r)(b_s^o - b_h^o) > n[\tau_{2s}^o L(\tau_{2s}^o) - \tau_{2h}^o L(\tau_{2h}^o)] > 0\). Remember that both types of regions are on the increasing side of the Laffer curve and \(\tau_{2s}^o > \tau_{2h}^o\). Thus, \(b_s^o > b_h^o\). \(g_{1s}^o = g_{1h}^o\) and \(\tau_{1s}^o = \tau_{1h}^o\) implies \(z_s^o = z_h^o + b_h^o - b_s^o < z_h^o\). By (5) we obtain \(z_s^o < 0 < z_h^o\). It remains to check the incentive compatibility constraints. Using the information derived so far, we can write \(V(b_s^o, z_s^o, \delta_s) - V(b_h^o, z_h^o, \delta_s) = \delta_s[P(\tau_{2s}^o) + U(g_{2s}^o) - P(\tau_{2h}^o) - U(g_{2h}^o)]\) with \(P(\tau) := (1 - \tau)L(\tau) + W[1 - L(\tau)]\) and \(P_0(\tau) = -L(\tau) < 0\). \(g_{2s}^o < g_{2h}^o\) and then imply \(V(b_s^o, z_s^o, \delta_s) - V(b_h^o, z_h^o, \delta_s) < 0\), i.e. (IC\(_s\)) is violated. By the same argument, we immediately obtain \(V(b_s^o, z_s^o, \delta_h) - V(b_h^o, z_h^o, \delta_h) = \delta_h[P(\tau_{2h}^o) + U(g_{2h}^o) - P(\tau_{2s}^o) - U(g_{2s}^o)] > 0\) so that (IC\(_h\)) is satisfied.

Proposition 1 states that, under full information, the intertemporal provision of the public good is undistorted. In both types of regions, the intertemporal rate of substitution between the public good in period 1 and the public good in period 2 equals the intertemporal rate of transformation. Since all regions have the same marginal utility of first-period consumption, the quantity of the public good and the tax rate in period 1 are the same across regions. In contrast, the discounted marginal utility of second-period consumption is higher for \(h\)-regions than for \(s\)-regions. High-preference regions realize a lower tax rate and a higher quantity of the public good in period 2. To finance the higher consumption, the center redistributes from low-preference regions (contributors) to high-preference regions (recipients). Moreover, debt of \(s\)-regions is higher than that of \(h\)-regions. While this insight implies that contributors are allowed to issue more debt than recipients, it is important to note that it does not yet make the
point for differentiated borrowing constraints. As will be shown in the next section, the full information optimum can be implemented without any budget institutions.

Let us now turn to the case of asymmetric information. Since the rate of time preference is private information, a region of a given type can mimic a region of the other type. As shown in Proposition 1, this information structure implies that the full information optimum is not incentive compatible. It satisfies the incentive constraint of h-regions, but violates that of s-regions. Low-preference regions have to finance the federal redistribution and, thus, by mimicking high-preference regions they receive a federal transfer and increase their welfare. To ensure incentive compatibility, the center has to change the optimal contracts such that both incentive constraints are satisfied. Denoting optimal values under asymmetric information by a star, we obtain

**Proposition 2.** The asymmetric information optimum satisfies

\[
\frac{U_g(g_{1s}^*)}{\delta U_g(g_{2s}^*)} = 1 + r, \quad \frac{U_g(g_{1h}^*)}{\delta h U_g(g_{2h}^*)} > 1 + r
\]

and \(g_{1s}^* > g_{1h}^*, \tau_{1s}^* < \tau_{1h}^*, g_{2s}^* < g_{2h}^*, \tau_{2s}^* > \tau_{2h}^*, b_s^* > b_h^*\) and \(z_s^* < 0 < z_h^*\).

**Proof:** Suppose (IC\(_h\)) is not binding so that \(\mu_h = 0\). This will be proven below. It follows \(\mu_s > 0\) since otherwise (14) to (17) would yield the full information optimum which violates (IC\(_s\)) according to Proposition 1. (14) and \(\mu_h = 0\) immediately imply \(U_g(g_{1s}^*)/\delta U_g(g_{2s}^*) = 1 + r\). From (15) we obtain

\[
(m_h - \mu_s)U_g(g_{1h}^*) = (m_h \delta_h - \mu_s \delta_s)(1 + r)U_g(g_{2h}^*) > (m_h - \mu_s)\delta_h(1 + r)U_g(g_{2h}^*)
\]

since \(\delta_s < \delta_h\). (17) and \(\mu_h = 0\) imply \(m_h - \mu_s > 0\). Thus, \(U_g(g_{1h}^*)/\delta h U_g(g_{2h}^*) > 1 + r\). Solving (16) and (17) with respect to \(\lambda\) yields

\[
\frac{m_s + \mu_s}{m_s} U_g(g_{1s}^*) = \frac{m_h - \mu_s}{m_h} U_g(g_{1h}^*).
\]

Moreover, we have \((m_s + \mu_s)/m_s > 1 > (m_h - \mu_s)/m_h\) and, thus, \(U_g(g_{1s}^*) < U_g(g_{1h}^*)\). It follows \(g_{1s}^* > g_{1h}^*\). From (7) we obtain \(F(\tau_{1s}^*) = nU_g(g_{1s}^*) < nU_g(g_{1h}^*) = F(\tau_{1h}^*)\). This implies \(\tau_{1s}^* < \tau_{1h}^*\) since \(F'(\tau) > 0\). To prove \(b_s^* > b_h^*\) and \(z_s^* < 0 < z_h^*\), note first that (IC\(_s\)) is binding due to \(\mu_s > 0\). Hence, both contracts \((b_s^*, z_s^*)\) and \((b_h^*, z_h^*)\) lie on the same indifference curve of s-regions. In addition, \((b_s^*, z_s^*)\) lies at the minimum of this indifference curve according to \(U_g(g_{1s}^*)/\delta U_g(g_{2s}^*) = 1 + r\) and (10). The U-shape of
the indifference curve then implies \( z_s^* < 0 < z_h^* \). \((b_s^*, z_s^*)\) lies on the decreasing part of the indifference curve of \(h\)-regions since \(U_g(g_{1h}^*)/\delta_h U_g(g_{2h}^*) > 1 + r\). The single-crossing property \((12)\) then proves \(b_s^* > b_h^*\). Furthermore, \((IC_h)\) is satisfied as presupposed. It remains to show \(g_{2s}^* < g_{2h}^*\) and \(\tau_{2s}^* > \tau_{2h}^*\). \(b_s^* > b_h^*\) implies \(g_{2s}^* - g_{2h}^* < n[\tau_{2s}^* L(\tau_{2s}^*) - \tau_{2h}^* L(\tau_{2h}^*)]\). By this inequality, \(g_{2s}^* \geq g_{2h}^*\) would imply \(\tau_{2s}^* > \tau_{2h}^*\). Remember that both types of regions are on the increasing side of the Laffer curve. But by \((7)\), \(g_{2s}^* \geq g_{2h}^*\) also implies \(F(\tau_{2s}^*) = nU_g(g_{2s}^*) \leq nU_g(g_{2h}^*) = F(\tau_{2h}^*)\) and \(\tau_{2s}^* \leq \tau_{2h}^*\), a contradiction. It follows \(g_{2s}^* < g_{2h}^*\) and by equation \((7)\) \(\tau_{2s}^* > \tau_{2h}^*\). 

In the asymmetric information optimum characterized in Proposition 2, the intertemporal allocation in low-preference regions is still not distorted. This result reflects the no-distortion-at-the-top property in our model. Incentive compatibility is ensured by two other properties. First, low-preference regions obtain an informational rent in the sense that their public consumption is increased. Their first-period public good consumption is now larger than in \(h\)-regions. Note also that, in the first period, \(s\)-regions have the lower income tax rate and, thus, the higher pre- and after-tax labor income. Second, the intertemporal allocation in high-preference regions is distorted. The marginal rate of substitution between current and future public consumption exceeds the marginal rate of transformation. There is a tendency to underprovision in period 1 and overprovision in period 2, and high-preference regions are forced to lower their debt. This distortion makes it unattractive for \(s\)-regions to mimic \(h\)-regions.

Proposition 2 also shows that the information asymmetry does not change the direction of redistribution in the federation. Low-preference (high-income) regions are still the contributors and high-preference (low-income) regions the recipients. Therefore, the intertemporal allocation of contributors is undistorted while that of recipients is distorted in favor of future public consumption. This insight should be kept in mind since it is of crucial importance for the optimal design of budget institutions in the federation which we will now turn to.

5 Implementation

In the welfare analysis of the previous section, we implicitly assumed that the federal government can directly control the allocation in the federation, i.e. can directly choose...
the level of spending, taxation and borrowing in the regions. Such a setting can serve as a normative benchmark, but it is obviously not consistent with observed policies in real world federations. Federal governments are usually responsible for interregional redistribution only and regions have considerable autonomy in the choice of regional policies. In this section, we therefore analyze which redistribution scheme allows the federal government to implement the welfare optimum, if the spending, taxation and borrowing decisions are decentralized at the regional level.

We consider two redistribution schemes of the federal government listed in Table 2. Both schemes consists of a $c$- and a $r$-program. The $c$-program aims at contributors of the federal redistribution, i.e. $s$-regions. It contains a lump-sum tax which contributors have to pay to the federal government. The $r$-program is designed for recipients of the federal redistribution, i.e. $h$-regions. It comprises a lump-sum transfer which the federal government pays to recipients. Under redistribution scheme $R2$, the transfer is combined with a ceiling $\bar{b}$ on regional debt. The recipients’ debt must not exceed this limit. Note that the ceiling is applied only under the $r$-program. Regions facing the $c$-program may issue higher debt. Hence, scheme $R2$ resembles the fiscal institution which we found in the U.S. and the European Union since, roughly speaking, it implies that recipient regions face stricter borrowing restrictions than contributing regions.

The regions take as given the redistribution system of the federal government and choose public debt in order to maximize their own welfare. By this choice, the regions also implicitly determine their tax rates and quantities of the public good in both periods. Under the $c$-program, the budget constraints of a type $i$ region are represented

<table>
<thead>
<tr>
<th>redistribution scheme</th>
<th>$c$-program</th>
<th>$r$-program</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>lump-sum tax $z_c$</td>
<td>lump-sum transfer $z_r$</td>
</tr>
<tr>
<td>R2</td>
<td>lump-sum tax $z_c$</td>
<td>lump-sum transfer $z_r$</td>
</tr>
</tbody>
</table>
by (4) with \( z_i = -z_c \). Welfare maximization of this region can therefore be written as

\[
\max_{b_i} V(b_i, -z_c, \delta_i). \tag{18}
\]

Under the \( r \)-program of redistribution scheme R1, a region of type \( i \) faces the budget constraints in (4) with \( z_i = z_r \). It therefore solves the same problem as in (18) except for replacing \(-z_c\) by \( z_r \). If the region faces the \( r \)-program of redistribution scheme R2, it additionally has to account for the borrowing constraint \( b_i \leq \bar{b} \).

We again start with the case of full information. It is then straightforward to show that the federal government can attain the welfare optimum by the redistribution system R1: Suppose the center assigns the \( c \)-program to \( s \)-regions and the \( r \)-program to \( h \)-regions. The center is able to do so since it observes the type of a region. Using the envelope theorem, the first-order conditions of the regions’ welfare maximization problems become

\[
U_g \left[ nT^1(b_s,-z_c)L[T^1(b_s,-z_c)] + b_s - z_c \right] = \delta_s(1+r)U_g \left[ nT^2(b_s)L[T^2(b_s)] - (1+r)b_s \right],
\]

\[
U_g \left[ nT^1(b_h,z_r)L[T^1(b_h,z_r)] + b_h + z_r \right] = \delta_h(1+r)U_g \left[ nT^2(b_h)L[T^2(b_h)] - (1+r)b_h \right].
\]

If the federal government sets \( z_c = -z^o_s \) and \( z_r = z^o_h \), the above conditions match those of the full information welfare optimum listed in Proposition 1. It follows that the regions choose \( b_s = b^o_s \) and \( b_h = b^o_h \). This finding is summarized in

**Proposition 3.** Consider the case of full information and redistribution scheme R1. Set \( z_c = -z^o_s \) and \( z_r = z^o_h \). Then the full information optimum is attained.

The intertemporal allocation in the full information optimum is not distorted. Hence, as shown in Proposition 3, the federal government can implement this optimum by scheme R1 which contains non-distortionary instruments only. The center simply has to set the federal taxes and transfers equal to their full information levels. The regions then choose the optimal debt levels. Budget institutions are not needed to implement the optimum. Therefore, a federal system with lax borrowing rules for contributors and strict borrowing rules for recipients cannot be rationalized in case of full information.

Next turn to the implementation under asymmetric information. Under this information structure, we know from Proposition 1 and 2 that the full information optimum
is no longer feasible. The objective of the federal redistribution policy is then to implement the asymmetric information optimum. Since the federal government cannot observe the type of a region, a low-preference region may mimic a high-preference region in order to obtain the $r$-program instead of the $c$-program. The federal government has to shape its redistribution system such that incentive compatibility is guaranteed for both types of regions. We obtain

**Proposition 4.** Consider the case of asymmetric information. Then the asymmetric information optimum cannot be attained with redistribution scheme $R1$. Under redistribution scheme $R2$, set $z_c = -z_s^*$, $z_r = z_h^*$ and $b = b_h^*$. Then the asymmetric information optimum is attained.

**Proof:** Under scheme $R1$, the first-order conditions of the regions’ welfare maximization problems are $U_g(g_{1i}) = \delta_i(1 + r)U_g(g_{2i})$, $i = s, h$. This contradicts Proposition 2. To prove the result for redistribution system $R2$, note first that a $s$-region facing the $c$-program realizes $(b_s^*, z_s^*)$. Under the $r$-program, the $s$-region maximizes $V(b_s, z_h^*, \delta_s)$ subject to $b_s \leq b = b_h^*$. Using the envelope theorem, the derivatives of the region’s welfare function can be written as

$$V_b(b_s, z_h^*, \delta_s) = U_g \left[ nT^1(b_s, z_h^*)L[T^1(b_s, z_h^*)] + b_s + z_h^* \right] - \delta_s(1 + r)U_g \left[ nT^2(b_s)L[T^2(b_s)] - (1 + r)b_s \right], \quad (19)$$

$$V_{bb}(b_s, z_h^*, \delta_s) = \left[ 1 + nT_b^1(L^1 + \tau_{1s}L_r^1) \right] U_{gg}^1 - \delta_s(1 + r) \left[ - (1 + r) + nT_b^2(L^2 + \tau_{2s}L_r^2) \right] U_{gg}^2. \quad (20)$$

(8) and (9) imply $1 + nT_b^1(L^1 + \tau_{1s}L_r^1) > 0$ and $-(1 + r) + nT_b^2(L^2 + \tau_{2s}L_r^2) < 0$. Hence, $V_{bb}(\cdot) < 0$. Evaluating (19) at $b_s = b_h^*$ yields

$$V_b(b_h^*, z_h^*, \delta_s) = U_g(g_{1h}^*) - \delta_s(1 + r)U_g(g_{2h}^*) > U_g(g_{1h}^*) - \delta_h(1 + r)U_g(g_{2h}^*) > 0. \quad (21)$$

The last inequality in (21) follows from Proposition 2. (21) together with $V_{bb}(\cdot) < 0$ implies $V_b(b_s, z_h^*, \delta_s) > 0$ for all $b_s \leq b_h^*$. Hence, under the $r$-program the $s$-region chooses $b_s = b_h^*$ and realizes $(b_h^*, z_h^*)$. But we know from Proposition 2 that it is
indifferent between \((b_s^*, z_s^*)\) and \((b_h^*, z_h^*)\). It therefore has no incentive to mimic a \(h\)-region, and redistribution system R2 is incentive compatible for \(s\)-regions.

Now turn to a \(h\)-region and suppose first it faces the \(r\)-program. It then maximizes \(V(b_h, z_h^*, \delta_h)\) subject to \(b_h \leq \bar{b} = b_h^*\). The derivatives of \(V\) are analogous to (19) and (20). Evaluating the first derivative at \(b_h = b_h^*\) yields

\[
V_b(b_h^*, z_h^*, \delta_h) = U_g(g_{1h}^*) - \delta_h(1 + r)U_g(g_{2h}^*) > 0. \tag{22}
\]

We obtain \(V_b(b_h, z_h^*, \delta_h) > 0\) for all \(b_h \leq b_h^*\). This means that the \(h\)-region sets \(b_h = b_h^*\) and realizes \((b_h^*, z_h^*)\). It has no incentive to mimic a \(s\)-region since \(V_b(b_h, z_s^*, \delta_h) > V_b(b_h, z_h^*, \delta_h)\) for all feasible \(b_h\). Redistribution system R2 is therefore incentive compatible for \(h\)-regions, too.

Redistribution scheme R1 leaves undistorted the intertemporal spending decisions of all regions. But the asymmetric information optimum is characterized by a distortion of the spending decisions of high-preference regions. This is the reason why the federal government cannot use scheme R1 to attain maximum welfare under asymmetric information. In contrast, the limit on regional debt under redistribution policy R2 restricts debt of recipient regions and so distorts their spending decisions in favor of future public consumption. The debt ceiling also makes the \(r\)-program unattractive for contributors. They voluntarily pay the lump-sum tax under the \(c\)-program instead of mimicking \(h\)-regions. By these two properties, the redistribution system R2 implements the welfare optimum under asymmetric information.

This insight may help to justify the differentiated budgetary institutions we observe in many real world federations. The ceiling on regional debt in our model applies to recipient regions only. Contributing regions are not restricted in choosing their debt level and therefore face less stringent budgetary institutions than recipients. Since contributing regions are the high-income regions in the asymmetric information optimum, the theoretical result also matches our empirical finding that budget institutions are less stringent in regions with above average personal income. The main argument our theoretical analysis provides for differentiated budget rules is that they help to solve the self-selection problem of the federal government in the presence of asymmetric information. With relatively lax borrowing rules for contributors and with suitable federal transfers, each region has an incentive to truthfully reveal its type and to implement the asymmetric information welfare optimum.
With respect to the U.S. evidence, it might be seen critical that in our model the budget institutions are part of the federal redistribution system while in reality they are set by the states themselves. But this is only a matter of interpretation. Under asymmetric information, a region of a given type can mimic a region of the other type. It can effectively choose between the c- and the r-program and, thus, it also has a choice between lax and strict borrowing rules. In this sense, the redistribution system R2 can be interpreted as pork barrel policy between the federal and the regional governments. The center redistributes resources into a region, but only if the region chooses budgetary institutions which prevent excessive public debt. Otherwise, the region is forced to pay the transfer from which the federal government finances the interregional redistribution.

6 Extensions and Modifications

In this section, we will briefly discuss the robustness of our results by extending or modifying the basic model. Since the formal proofs of the results are quite similar to the proofs of Proposition 1 to 4, we only report on the results and explain their intuition. Detailed proofs can be obtained upon request.

As a first extension, suppose the federal government maximizes the weighted Utilitarian welfare function \( \gamma m_s V(b_s, z_s, \delta_s) + (1 - \gamma) m_h V(b_h, z_h, \delta_h) \) with \( \gamma \in [0, 1] \). The welfare of low-preference regions is weighted by \( \gamma \), whereas the welfare of high-preference regions enters the social welfare function with the weight \( 1 - \gamma \). This welfare function is more general than (13) since by varying the parameter \( \gamma \) we can attain every point on the Pareto utility frontier of the federation. With \( \gamma = 0.5 \), both types of regions receive the same welfare weights and we obtain exactly the same results as under the social welfare function (13). But in the general case, there exists a \( \tilde{\gamma} \in [0.5, \delta_h/(\delta_s + \delta_h)] \) such that three cases have to be distinguished: case 1 with \( \gamma \in [0, \tilde{\gamma}] \), case 2 with \( \gamma \in [\tilde{\gamma}, \delta_h/(\delta_s + \delta_h)] \) and case 3 with \( \gamma \in [\delta_h/(\delta_s + \delta_h), 1] \).

In case 1, the full information optimum can be shown to satisfy \( g_{2s}^o < g_{2h}^o \) and \( \tau_{2s}^o > \tau_{2h}^o \) since the 'weighted' discount factor in \( h \)-regions, \( (1 - \gamma)\delta_h \), is larger than the one in \( s \)-regions, \( \gamma\delta_s \). For \( \gamma \in [0, 0.5] \) we additionally have \( g_{1s}^o \leq g_{1h}^o \) and \( \tau_{1s}^o \geq \tau_{1h}^o \) since the welfare weight of \( s \)-regions is not larger than that of \( h \)-regions. In this
subcase, (IC_h) obviously is satisfied while (IC_s) is not. Though $\gamma \in ]0.5, \bar{\gamma}[ \implies g^0_s > g^0_h$ and $\tau^0_s < \tau^0_h$, the incentives properties of the full information optimum are the same as in the subcase $\gamma \in ]0,0.5]$. The welfare weight $\gamma$ is still sufficiently low so that mimicking is profitable for a s-region since the welfare gain in period 2 outweighs the welfare loss in period 1. Hence, in case 1 the full information optimum is always incentive compatible for high-preference regions, but not for low-preference regions. This property ensures that the results derived in the previous sections remain true. The asymmetric information optimum distorts the intertemporal allocation in $h$-regions and the center can implement this optimum by redistribution scheme R2. Thus, the optimality of a redistribution system with laxer budget institutions for contributors than for recipients can be generalized to a wide class of social welfare function.

Unfortunately, a further generalization to the cases 2 and 3 is not possible. Since the welfare weight of s-regions is relatively high in these cases, the incentive properties of the full information optimum change. In case 2, the full information optimum satisfies the incentive constraints of both types of regions. The asymmetric information optimum is identical to the full information optimum and the federal government can implement the optimum without borrowing constraints. In case 3, the welfare weight of s-regions is so high that the full information optimum satisfies (IC_s), but not (IC_h). The asymmetric information optimum distorts the spending decisions of s-regions which are now the recipients. But the distortion is in favor of current consumption. The center can therefore implement the asymmetric information optimum by a redistribution system which comprises a floor on the recipients’ debt. This result would contrast the result in case 1 since the redistribution system now allows for relatively lax budget rules in recipient regions, not in contributing regions. But floors on public debt are rarely observed and hardly imaginable from an empirical point of view.

For the second modification of our basic model, we return to the welfare function (13), but consider another source of information asymmetry. In the previous fiscal federalism literature, it is often argued that the federal government cannot observe the labor productivity in a region. For instance, Bordignon et al. (2001) suppose the representative individuals of the regions differ in their effective time endowment and the center cannot infer this productivity parameter. Analogously, in our model we may assume that the time endowment is the same for the first-period individuals, but
not for the second-period individuals. The time constraints in period 1 and 2 then read \( \ell_{1i} + x_{1i} = 1 \) and \( \ell_{2i} + x_{2i} = 1 + e_i \) with \( 0 < e_s < e_h \), i.e. \( s \)-regions have low and \( h \)-regions high labor productivity. Focusing on differences in period 2 is clearly simplifying. However, it allows to model in a stylized way the fact that information asymmetries with respect to future regional characteristics are usually more severe than information asymmetries with respect to current characteristics.\(^6\)

In a model with differences in the labor productivity, we obtain qualitatively the same results as in the basic model with different rates of time preference. Under full information, optimal redistribution is from high-productivity to low-productivity regions. The welfare optimum is incentive compatible for recipients, but not for contributors. Consequently, the asymmetric information optimum distorts the intertemporal allocation of low-productivity regions, and the center can implement this asymmetric information optimum by imposing a debt limit on low-productivity regions. Hence, we again obtain the result that lax budget rules for contributors and strict budget rules for recipients solve the self-selection problem of the federal government.

As a final modification, we consider a third source of information asymmetry. Previous studies referred to in the introduction argue that the cost of the regional public good supply cannot be observed by the federal government. Focusing again on the more serve information problem in period 2, we may suppose that regions have different unit cost of the public good in the second period. Denote unit cost of a type \( i \) region by \( \theta_i \) with \( \theta_s < \theta_h \). The budget constraints of region \( i \) then read \( g_{1i} = n\tau_{1i}L(\tau_{1i}) + b_i + z_i \) and \( \theta_i g_{2i} = n\tau_{2i}L(\tau_{2i}) - (1 + r)b_i \). In this setting, it can be shown that the direction of redistribution in the federation is determined by the elasticity of the marginal utility of the public good, \( \eta := -gU_{gg}/U_g \). If the center reallocates one unit of the public good in period 2 from \( h \)- to \( s \)-regions, it gains the difference in marginal cost, but losses the difference in marginal utility of the public good. For \( \eta < 1 \), the former effect dominates the latter and redistribution in the full information optimum is from \( h \)- to \( s \)-regions. If \( \eta > 1 \), the reverse is true, and \( \eta = 1 \) implies that there is no redistribution at all.

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\(^6\)Official statistics and short-run forecasts provide the federal government data which exhibit informational problems, indeed, but the reliability of these data is surely higher than that of the data obtained from long-run forecasts. Regional governments are usually better informed about, for example, the long-run demographic change or other regional developments which influence labor productivity. This information advantage of the regions is surely smaller in the short-run.
Independent of the direction of redistribution, however, the incentive properties of the full information optimum are almost always the same. Except for the pathological case $\eta = 1$, the full information optimum can be shown to satisfy the incentive constraint of recipients and to violate that of contributors. Under asymmetric information, the intertemporal spending decisions of recipients are distorted in favor of future public consumption and the federal government implements this optimum by redistribution scheme R2. Hence, redistribution systems with relatively lax budget institutions for contributors are again efficient.

7 Conclusion

This paper developed a two-period model of a federation consisting of a federal government and several regions. Each region provides a public good financed by a distortionary income tax and, in the first-period, by public debt and a federal transfer. The regions differ with respect to the rate of time preference and the federal government redistributes from low-preference to high-preference regions. In the full information welfare optimum, the intertemporal allocation is undistorted in each region. This optimum can be implemented by a simple redistribution scheme consisting of lump-sum taxes and transfers. But under asymmetric information, the welfare optimum is characterized by a distortion of the intertemporal allocation in recipient regions. The center attains this welfare optimum, if it augments the redistribution scheme by a limit on the borrowing of recipients. This ensures incentive compatibility for contributors.

Although we already showed that these results are quite robust with respect to variations in the shape of the social welfare function and the source of the information asymmetry, there are further sensible extensions of our analysis. Perhaps most interestingly, we considered the different sources of information asymmetry only separately. But the federal government often cannot observe several characteristics of the regions. So, our analysis may be extended to a two- or multidimensional screening problem where the federal government cannot infer, for example, the rate of time preference and labor productivity. The question is then under what conditions our result prevails and under what conditions it breaks down. These conditions may then provide further insights in the variation of budget rules in real world federation.
References


